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Chapter 7: Right Triangles
Topic 1: Plane Geometry
Common "Things" to know for this lesson:

1) Line:

2) Point:

0
3) Intersecting Lines:

4) Plane:

5) Parallel:

6) Perpendicular:

7) Coplanar:

8) Collinear:


## PLANE THEOREMS!!

1. If a line is perpendicular to a plane at a given point, it is perpendicular to every line in the plane which passes through that point.


## If $t \perp l$ then $t \perp A B$ and $t \perp C D$

3. Given a point on a plane, there is only one line that can be drawn perpendicular to the plane that passes through the given point.


## Given point A on plane l, only BC $\perp l$

5. Given two lines perpendicular to the same plane, the two lines are said to be coplanar (lie in the same plane.)

$A B \perp q$ and $C D \perp q$, then $A B$ and $C D$ are both contained in plane l
6. If a given line is perpendicular to a plane, then any line that is perpendicular to the given line at its point of intersection with the given plane is in the given plane.


## If $A B \perp l$, at point $B$, then $B C$

$\perp A B$ at $B$, and $B$ is contained in plane $l$
2) If a line is perpendicular to each of two intersecting lines at their point of intersection, it is Also perpendicular to the plane which contains those lines.


$$
\text { If } t \perp A B \text { and }
$$

t. $\perp . C D$ at the point of intersection then $t . \perp$ l.
4. Given a point NOT on a plane, there is only one line that can be drawn perpendicular to the plane that passes through the given point.


## Given point B NOT on plane l, only BAC $\perp l$

6. If one plane contains a line perpendicular to the second plane, then the two planes are perpendicular to each other.


$$
\text { If } A B \perp l \text {, then } q \perp l
$$

8. If a line is perpendicular to a plane, then every plane containing the line is perpendicular to the given plane.


If $A B \perp l$, then $q \perp l$
9. If a plane intersects two parallel planes, then the intersection is two parallel lines.

Note: The intersection of the two planes always forms a line.


If $l \| r$, then $A B \| C D$
11. If two or more lines are perpendicular to the same plane, then the two lines are parallel to each other.

10. If two planes are perpendicular to the same line, then the given planes are parallel.


$$
\text { If } l \perp D C \text { and } l_{1} \perp D C \text {, then } l \| l_{1}
$$

12. If two lines which intersect a plane are parallel to a third line which also intersects the plane, the lines are parallel to each other.


## Examples:

1) If two points lie in a plane the line joining them also lies in the same plane
(a) True
(b) False
2) Point $P$ is on line $m$. What is the total number of planes that are perpendicular to line $m$ and pass through point P.
(a) 1
(b) 2
(c) 0
(d) infinite
3) In three-dimensional space, two planes are parallel and a third plane intersects both of the parallel planes. The intersection of the planes is a:
(a) plane
(b) point
(c) pair of parallel lines
(d) pair of intersecting lines
4) Line $k$ is drawn so that it is perpendicular to two distinct planes, $P$ and $R$. What must be true about planes $P$ and R?
(a) Planes P and R are skew
(b) Planes P and R are parallel
(c) Planes $P$ and $R$ are perpendicular
(d) Plane $P$ intersects Plane $R$ but is not perpendicular
5) Given point $P$ is on plane R. What is the total number of lines that can be drawn that are perpendicular to plane $R$ and pass through point $P$.
(a) 1
(b) 2
(c) 0
(d) infinite
6) If two lines are perpendicular to the same plane they:
(a) are perpendicular
(b) are parallel
(c) intersect but are not perpendicular
(d) none of the above
7) Lines $k_{1}$ and $k_{2}$ intersect at point E . Line m is perpendicular to lines $k_{1}$ and $k_{2}$ at point E .

(a) Lines $k_{1}$ and $k_{2}$ are perpendicular
(b) Line m is parallel to the plane determined by lines $k_{1}$ and $k_{2}$
(c) Line $m$ is perpendicular to the plane determined by lines $k_{1}$ and $k_{2}$
(d) Line m is coplanar with Lines $k_{1}$ and $k_{2}$
8) State the answer as either: parallel or perpendicular

If line $A B$ and $C D$ are parallel lines, and plane $P$ is perpendicular to the line $A B$, then plane $P$ must be
$\qquad$ to line CD.
$\qquad$
$\qquad$

## Plane Geometry: Homework

Complete the following questions below, circle your answer.
1.) Plane $P$ is parallel to plane $Q$. If plane $P$ is perpendicular to line $l$, then plane $Q$
(1) contains line $l$.
(2) is parallel to line $l$.
(3) is perpendicular to line $l$.
(4) intersects, but is not perpendicular to line $l$.
2.) In the diagram below, point $K$ is in plane $P$. How many lines can be drawn through $K$, perpendicular to plane $P$.
(1) 1
(2) 2
(3) 0
(4) an infinite number

3.) If distinct plane $R$ and $S$ are both perpendicular to line $l$, which statement must always be true?
(1) Plane $R$ is parallel to plane $S$.
(2) Plane $R$ is perpendicular to plane $S$.
(3) Planes $R$ and $S$ and line $l$ are all parallel.
(4) The intersection of planes $R$ and $S$ is perpendicular to line $l$.
4.) If line $l$ is perpendicular to distinct planes $P$ and $Q$, then planes $P$ and $Q$
(1) are parallel.
(2) contain line $l$.
(3) are perpendicular.
(4) intersect, but are not perpendicular.
5.) Point $A$ is on line $m$. How many distinct planes will be perpendicular to line $m$ and pass through point A?
(1) one
(2) two
(3) zero
(4) infinite
6.) Plane $A$ and plane $B$ are two distinct planes that are both perpendicular to line $l$. Which statement about planes $A$ and $B$ is true?
(1) Planes A and B have a common edge, which forms a line.
(2) Planes A and B are perpendicular to each other.
(3) Planes A and B intersect each other at exactly one point.
(4) Planes A and B are parallel to each other.
7.) As shown in the diagram below, $\overline{F D}$ and $\overline{C B}$ intersect at point A and $\overline{E T}$ is perpendicular to both $\overline{F D}$ and $\overline{C B}$ at A . Which statement is not true?
(1) $\overline{E T}$ is perpendicular to plane BAD.
(2) $\overline{E T}$ is perpendicular to plane FAB .
(3) $\overline{E T}$ is perpendicular to plane CAD.
(4) $\overline{E T}$ is perpendicular to plane BAT.


## Review Questions:

8.) After the transformation $r_{y=x}$, the image of $\triangle A B C$ is $\Delta A^{\prime} B^{\prime} C^{\prime}$. If $A B=2 \mathrm{x}+13$ and $A^{\prime} B^{\prime}=9 x-8$, find the value of $x$.
9.) In $\triangle A B C, m \angle A=x^{2}+12, m \angle B=11 x+5$, and $m \angle C=13 x-17$. Determine the longest side of $\triangle A B C$.

