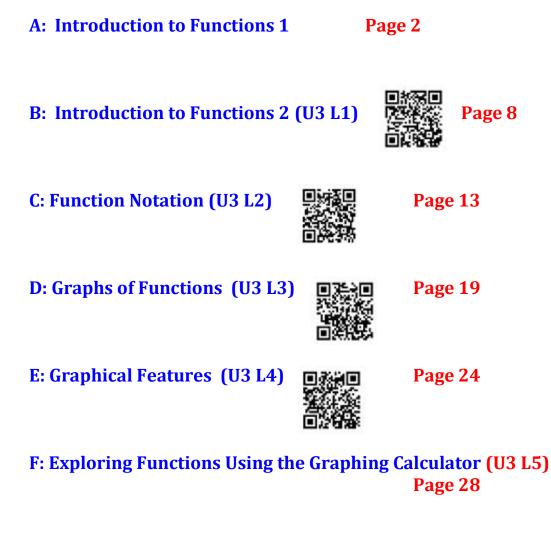
Packet 4: Functions

Index:



G: Average Rate of Change (U3 L6)



H: The Domain and Range of a Function (U3 L7)



Page 38

Relations & Functions

A <u>relation</u> is a set of ordered pairs. *Example*: $\{(-3, -1), (-1,9), (0, -7), (4,7), (4,9), (5, -2)\}$

The **domain** is the set of all of the x-coordinates from the ordered pairs.

Ex: _____

The **<u>range</u>** is the set of all of the y-coordinates from the ordered pairs.

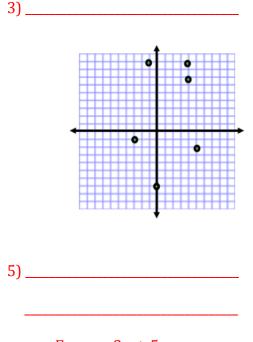
Ex:_____

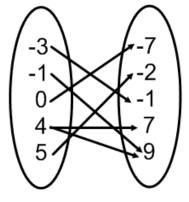
The **graph of a relation** is the set of points on a graph equivalent to the ordered pairs in the relation.

4)

Options for representing a relation

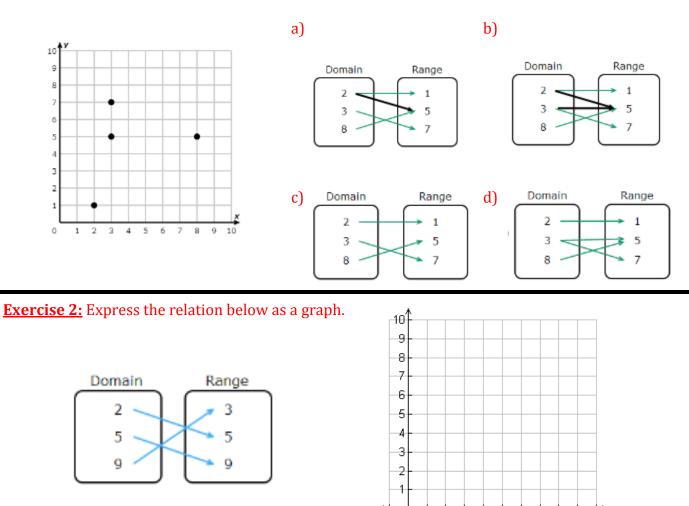
2)			
	x	y	
	-3	-1	
	-1	9	
	0	-7	
	4	7	
	4	9	
	5	-2	





Ex: y = 3x + 5 $y = 2x^2 + 3x - 7$

Exercise 1:Using the provided graph, which mapping represents the relation?



Relations vs. Functions

-1

23

56

4

Relations: A relation is simply a set of ordered pairs. A relation can be any set of ordered pairs and no special rules are applied.

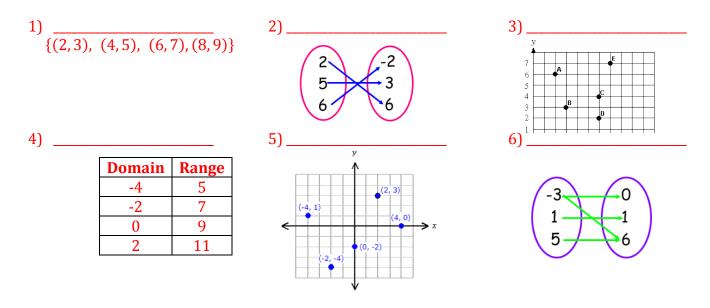
Functions: A function is a set of ordered pairs (relation), in which each x – element has ONE y – element associated with it. *(no x repeats)*

9 1D

8

7

Exercise 3: Identify each of the following as a relation or function.



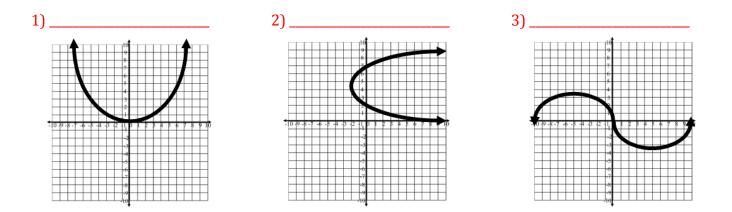
Exercise 4: Answer the following questions:

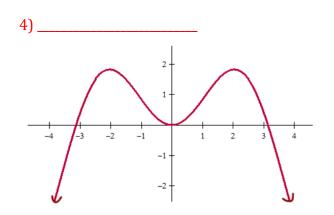
- 1) Given the relation $B = \{(5,2), (7,4), (9,10), (x,5)\}$ Which of the following values for x will make relation B a function?
 - (1) 7 (2)9 (3) 4 (4) 5
- _____2) The following relation is a function. {(10,12), (5,3), (15,10), (5,6), (1,0)} (1) true (2) false
- _____ 3) Is the relation depicted in the chart below a function?

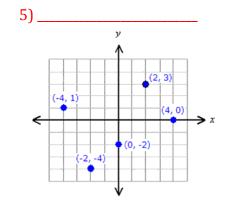
	x	0	1	3	5	3	9
	y	8	9	10	6	11	7
(1) yes	5				(2) no	

Vertical Line Test: When examining a graph to determine if it is a relation or function, a vertical line can be drawn through the graph. If the vertical line intersects the graph once, then the graph is a function and if the vertical line intersects the graph more than once, the graph is a relation.

Exercise 5: Identify each of the following as a relation or function.







Na	me:_

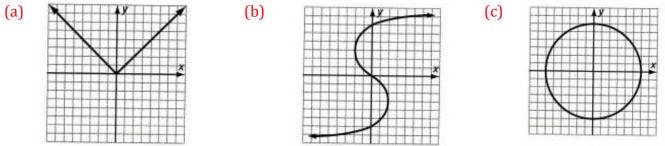
Algebra I

_____1) Is the relation depicted in the chart below a function?

- /			1					
	x	1	2	3	4	5	6	
	у	4	5	6	7	8	9	
	(1)	yes			(2) no		
2) Wł	nich of	the r	elat	ions is	s a fu	inctio	n?	
(1)	{(1,3),	(2,4	4), ((3,1),	(3,2), (4,	4)}	
(2)	{(0,3),	(1,4	4), ((1,1),	(2,2), (3,	5)}	
(3)	{(0,3),	(1,4	4), ((2,1),	(3,2), (2,	3)}	
(4)	{(1,3),	(2,4	4), ((3,1),	(4,2), (5,	3)}	
3) Wł	nich of	the r	elat	ions is	s <u>not</u>	<u>t</u> a fu	nctio	n?

- (1) {(1,3), (2,4), (3,1), (4,2), (5,4)}
- $(2) \{ (0,3), (2,4), (1,1), (5,2), (3,5) \}$
- $(3) \{(0,3), (1,4), (2,1), (3,2), (2,3)\}$
- $(4) \ \{(1,3), \ (2,4), \ (3,1), \ (4,2), \ (5,3)\}$
- 4) In 2013, the United States Postal Service charged \$0.46 to mail a letter weighing up to 1 oz. and \$0.20 per ounce for each additional ounce. Which function would determine the cost, in dollars, c(z), of mailing a letter weighting z ounces where z in an integer greater than 1?
 - (1) c(z) = 0.46z + 0.20 (2) c(z) = 0.20x + 0.46(2) c(z) = 0.46(z - 1) + 0.20 (4) c(z) = 0.20(z - 1) + 0.20
 - (3) c(z) = 0.46(z-1) + 0.20 (4) c(z) = 0.20(z-1) + 0.46
- _____5) Which of the ordered pairs is <u>not</u> a function?
 - $(1) \{(0,9), (9,0), (1,2), (3,4)\}$
 - (2) {(0,1), (-1,0), (1,2), (3,2)}
 - $(3) \{(2,3), (3,4), (4,5), (5,6)\}$
 - $(4) \{ (2,3), (2,4), (4,5), (5,6) \}$
 - 6) If the function *h*(*x*) represents the number of full hours that it takes a person to assemble x sets of tires in a factory, which would be an appropriate domain for the function?
 - (1) the set of real numbers
 - (2) the set of negative numbers
 - (3) the set of integers
 - (4) the set of non-negative integers

7) Use the vertical line test to determine if it is a function.



Review Section:

8) (a) Solve the following inequality: $-6x + 10 \le 34$

(b) What is the smallest value of x to make this inequality true?

Name:	Date:_	Period:	
Algebra I	Introd	uction to Functions 2	3B

The concept of the function ranks near the top of the list in terms of important Algebra concepts. Almost all of higher-level mathematical modeling is based on the concept. Like most important ideas in math, it is relatively simple:

THE DEFINITION OF A FUNCTION

A function is a clearly defined rule that converts an input into at most *one output*. These rules often come in the form of: (1) equations, (2) graphs, (3) tables, and (4) verbal descriptions.

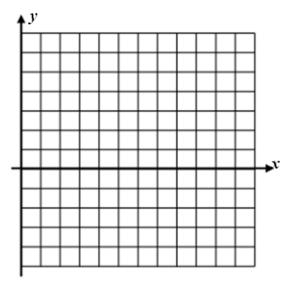
Exercise #1: Consider the function rule: multiply the input by two and then subtract one to get the output.

(a) Fill in the table for the inputs and outputs. Inputs are often designated by *x* and outputs by *y*.

Input	Calculation	Output
x		<u>y</u>
0		
1		
2		
3		

(b) Write an equation that gives this rule in symbolic form.

(c) Graph the function rule on the graph paper shown below. Use your table in part a to help.



Exercise #2: In the function rule from #1, what input would be needed to produce an output of 17? Why is it harder to find an input when you have an output than finding an output when you have an input?

Exercise #3: A function rule takes an input, n, and converts it into an output, y, by increasing one half of the input by 10. Determine the output for this rule when the input is 50 and then write an equation for the rule in symbolic form.

Exercise #4: Function rules do not always have to be numerical in nature, they simply have to return a single output for a given input. The table below gives a rule that takes as an input a neighborhood child and gives as an output the month he or she was born in.

Child	Birth Month
Max	January
Evin	April
Zeke	May
Rosie	February
Niko	May

(b) What is the output when the input is Rosie?

(a) Why can we consider this rule a function?

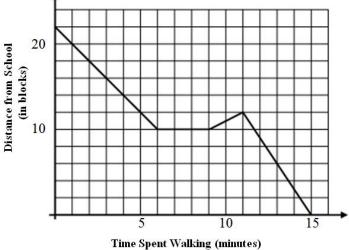
(c) Find all inputs that give an output of May. Why does this *not* violate the definition of a function even though there are two answers?

Functions are useful because they can often be used to model things that are happening in the real world. The next exercises illustrates a function given only in graphical form.

Exercise #5: Charlene heads out to school by foot on a fine spring day. Her distance from school, in blocks, is given as a function of the time, in minutes, she has been walking. This function is represented by the graph given below. (a) How far does Charlene start off from school?

(b) What is her distance from school after she has been walking for 4 minutes?

(c) After walking for six minutes, Charlene stops to look for her subway pass. How long does she stop for?



(d) Charlene then walks to a subway station before heading to school on the subway (a local). How many blocks did she walk to the subway? (e) How long did it take for her to get to school once she got on the train?

Name:	Date: Period:	
Algebra I	Introduction to Functions 2	3B HW

1.) Decide whether each of the following relations is a function. Explain your answer.

Input	Output	Function?
States	Capitals	
States	Cities	
Families	Pets	
Families	Last names	

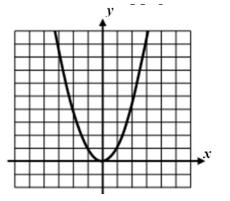
2.) In each of the following examples, use an input-output chart to decide if the following relation is a function.(a) Consider the following relation: multiply the(b) Consider the following table:

input by five and then subtract seven to get the output. Function? Yes or No? (b) Consider the following table: Function? Yes or No?

Input	Calculation	Output
x		y
-3		
0		
6		

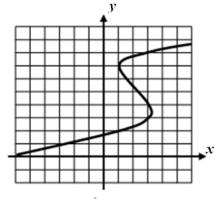
Input	Calculation	Output
x		У У
-2	None	4
3	None	3
3	None	2

(c) Consider the following graph. Function? Yes or No?



Input	Calculation	Output(s)
x		y
-2	None	
1	None	
2	None	

(d) Consider the following graph. Function? Yes or No?



Input	Calculation	Output(s)
x		y
-3	None	
1	None	
3	None	

3.) Andrew has a new job at the local pizza store as a delivery boy. The following graph shows one of his deliveries he made. Analyze the graph and answer the following questions.

(a) How long was the entire delivery trip?

(b) If he arrived at the house after 4 minutes, how far away was the house from the pizza place?

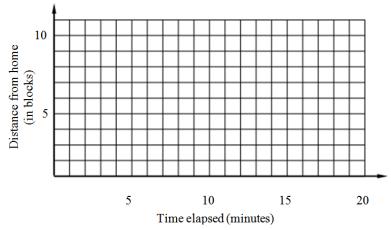
(c) Why might Andrew have stopped 3 times for 1 minute?

by the second se

(d) Was Andrew's trip longer going to the house or coming back?

4.) Given the following scenario, graph a function that would map Liza's distance away from her house according to the time elapsed.

Liza has a few items she needs to pick up from a grocery store 8 blocks away. Liza travels as a constant rate of 2 blocks per minute when not stopped at a light. On her way to the grocery store she doesn't hit any red lights and the trip takes her 4 minutes. She spends 8 minutes in the grocery store and then starts to head home. When she's halfway home she hits a red light that lasts 3 minutes. After the light ends, she then drives the second half of the way home.



 Review Section:

 5.) Which value of x is the solution of $\frac{1}{5} + \frac{2}{x} = \frac{1}{3}$?

 $[1] -2\frac{3}{4}$ [2] -15

 $[3] 2\frac{3}{4}$ [4] 15

6.) The product of a number and 3, increased by 5, is 7 less than twice the number. Which equation can be used to find this number, *n*?

7.) Which value	e of x is a solution of the inequality $25x - 100 < 250$?
[1] 13	[2] 14
[3] 15	[4] 16

8.) A total of 1680 ounces of pet food have to be packed in 5-pound bags. How many 5-pound bags of pet food can be packed?

	1 pound =	16 ounces
[1] 2	1	[2] 28
[3] 1	.05	[4] 336

9.) The equation (x - 6)(x + 8) = (x - 6)(8) + (x - 6)(x) illustrates the use of which property?

[1] distributive property

[2] associative property of addition

[3] associative property of multiplication

[4] commutative property of multiplication 2

10.) If $(7.6 \times 10^n)(3.5 \times 10^3) = 2.66 \times 10^9$, what is the value of *n*? [1] 6 [2] 5 [3] 3 [4] 7

Name:	Date: Period:	
Algebra I	Function Notation	3C

Since functions are rules that convert **inputs** (typically *x*-values) into **outputs** (typically *y*-values), it makes sense that they must have their own **notation** to indicate what the what the rule is, what the input is, and what the output is. In the first exercise, your teacher will explain how to interpret this notation.

Exercise #1: For each of the following functions, find the outputs for the given inputs. (a) f(x) = 3x + 7 (b) $g(x) = \frac{x-6}{2}$ (c) $h(x) = \sqrt{2x+1}$ f(2) = g(20) = h(4) =f(-3) = g(0) = h(2) =

Function notation can be very, very confusing because it really looks like multiplication due to the parentheses. But, there is no multiplication involved. The notation serves two purposes: (1) to tell us what the rule is and (2) to specify an output for a given input.

FUNCTION NOTATION

$$y = f(x)$$

Output ______ Rule _____ Input

Exercise #2: Given the function $f(x) = \frac{x}{3} + 7$ do the following. (a) Explain what the function rule does to convert (b) Evaluate f(6) and f(-9). the input into an output.

(c) Find the input for which f(x) = 13. Show the work that leads to your answer

(d) If g(x) = 2 f(x) - 1 then what is g(6)? Show the work that leads to your answer.

Recall that function rules commonly come in one of three forms: (1) equations (as in Exercise #1), (2) graphs, and (3) tables. The next few exercises will illustrate function notation with these three forms. **Exercise #3**: Boiling water at 212 degrees Fahrenheit is left in a room that is at 65 degrees Fahrenheit and begins to cool. Temperature readings are taken each hour and are given in the table below. In this scenario, the temperature, *T*, is a function of the number of hours, *h*.

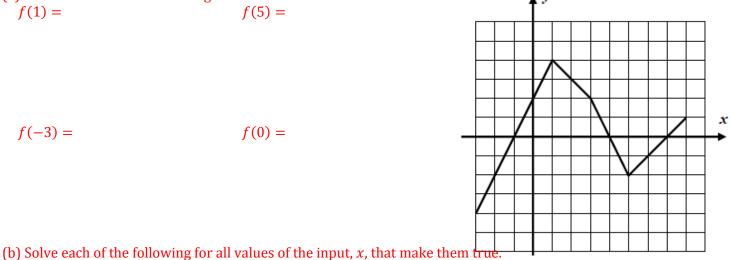
h (hours)	0	1	2	3	4	5	6	7	8
$ \begin{array}{c} T(h) \\ (°F) \end{array} $	212	141	104	85	76	70	68	66	65

(a) Evaluate T(2) and T(6)

(b) For what value of h is T(h) = 76?

(c) Between what two consecutive hours will T(h) = 100? Explain how you arrived at your answer.

Exercise #4: The function y = f(x) is defined by the graph shown below. It is known as **piecewise linear** because it is made up of **straight line segments.** Answer the following questions based on this graph. (a) Evaluate each of the following:



 $f(x) = 0 \qquad \qquad f(x) = 2$

(c) What is the largest output achieved by the function? At what x –value is it hit?

Name: Algebra I		Date: Function Nota	Period: tion	3C HW
1.) Given the function f (a) $f(4)$	defined by the formula $f(x)$ (b) $f(-5)$	x = 2x + 1 find the following (c) $f(0)$	$(d) f\left(\frac{1}{2}\right)$	

2.) Given the function g defined by the formula $g(x) = \frac{x-5}{2}$ find the following: (a) g(9) (b) g(0) (c) g(3) (d) g(17)

3.) Given the function h defined by the formula $h(x) = x^2 - 4$ find the following: (a) h(3)(b) h(-4)(c) h(0)(d) h(-2)

4.) If the function f(x) is defined by $f(x) = \frac{x}{2} - 6$ then which of the following is the value of f(10)? [1] -1 [2] 2 [3] 14 [4] 7

5.) If the function f(x) = 2x - 3 and $g(x) = \frac{3}{2}x + 1$ then which of the following is a true statement? [1] f(0) > g(0) [2] f(2) = g(2)[3] f(8) = g(8) [4] g(4) < f(4)

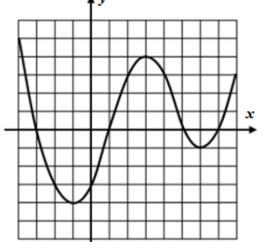
6.) Based on the graph of the function y = g(x) shown below, answer the following questions. (a) Evaluate each of the following. Illustrate with a point on the graph. y

$$g(-2) = g(0) =$$

 $g(3) = g(7) =$

(b) What values of x solve the equation g(x) = 0? These are called the zeros of the function.

(c) How many values of x solve the equation g(x) = 2? How can you illustrate your answer on the graph?



7.) Physics students drop a ball from the top of a 100 foot high building and model its height above the ground as a function of time with the equation $h(t) = 100 - 16t^2$. The height, *h*, is measured in feet and time, *t*, is measured in seconds. Be careful with all calculations in this problem and remember to do the exponent first! (a) Find the value of h(0) Include proper units What does this output represent? (b) Calculate h(2) Does our equation predict that the ball has hit the ground at 2 seconds? Explain.

8.) If you knew that f(-4) = 8, then what (x, y) coordinate point must lie on the graph of y = f(x)? Explain your reasoning.

Review Section:

- 9.) The length of a rectangle is represented by $x^2 + 3x + 2$ and the width is represented by 4x.
 - (a) Express the perimeter of the rectangle as a trinomial. (b) Express the area of the rectangle as a trinomial.

10.) The product of $6x^3y^3$ and $2x^2y$ is:[1] $3xy^2$ [2] $8x^5y^4$ [3] $12x^5y^4$ [4] $12x^6y^3$

 11.) It takes a snail 500 hours to travel 15 miles. At this rate, how many hours will it take the snail to travel 6 mi?

 [1] 0.18
 [2] 5.56

 [3] 150
 [4] 200

12.) What is the solution of $4x - 30 \ge -3x + 12$? [1] $x \ge 6$ [2] $x \le 6$ [3] $x \ge -6$ [4] $x \le -6$

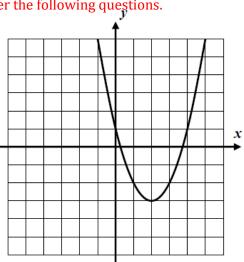
13.) Is the following considered a function? Explain why or why not. {(3,4),(-1,3),(3,5),(6,-1)}

Name:	Date: Period:	
Algebra I	Graphs of Functions	3D

Graphs are one of the most powerful ways of visualizing a function's rule because you can quickly read outputs given inputs. You can also easily see features such as maximum and minimum output values. Let's review some of those skills in Exercise #1.

Exercise #1: Given the function y = f(x) defined by the graph below, answer the following questions. (a) Find the value of each of the following: f(4) =f(-1) =



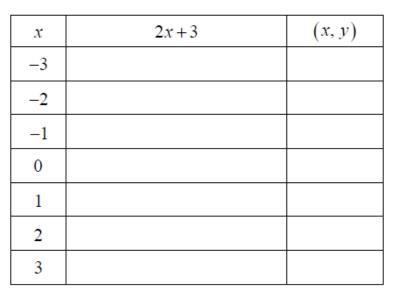


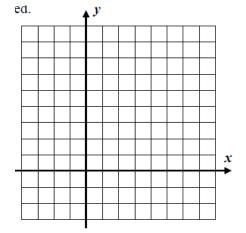
(c) State the minimum and maximum values of the function.

So, if we can read a graph to produce outputs (y-values) if we are given inputs (x-values), then we should be able to reverse the process and produce a graph of the function from its **algebraically expressed rule**.

Exercise #2: Consider the function given by the rule g(x) = 2x + 3(a) Fill out the table below for the inputs given.

h	Draw a	granh	of the	function	on the	granh
U		graph	or the	runction	on the	graph.

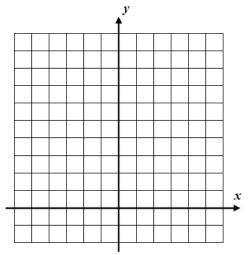




Never forget that all we need to do to **translate** between an equation and a graph is to **plot** input/output pairs according to whatever rule we are given. Let's look at a simple **non-linear** function next.

Exercise #3: Consider the simplest quadratic function $f(x) = x^2$. Fill out the function table below for the inputs given and graph the function on the axes provided.

x	x^2	(x, y)
-3		
-2		
-1		
0		
1		
2		
3		



Sometimes the function's rule gets all sorts of funny and can include being *piecewise defined*. These functions have different rules for different values of *x*. These separate rules combine to make a larger (and more complicated rule). Let's try to get a feel for one of these.

Exercise #4: Consider the function given by the formula $f(x) = \begin{cases} 2x + 6 & x < 0 \\ 6 - x & x \ge 0 \end{cases}$

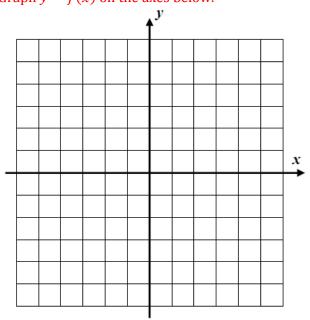
(a) Evaluate each of the following.

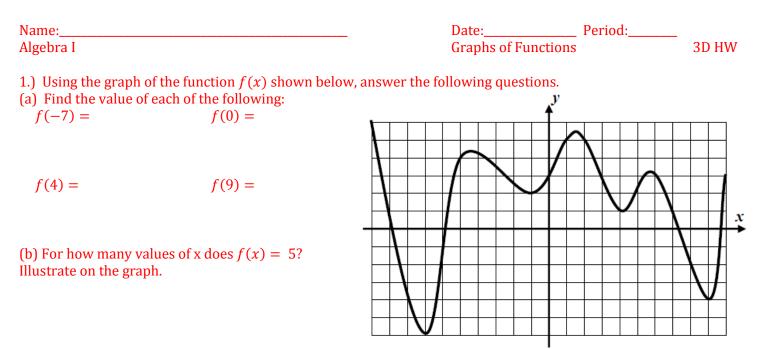
 $f(4) = \qquad \qquad f(-3) =$

(c) Graph y = f(x) on the axes below.

(b) Fill out the table below for the inputs given. Ke	ep
in mind which formula you are using.	

x	Rule/Calculation	(x, y)
-3		
-2		
-1		
0		
1		
2		
3		





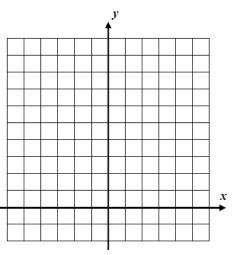
(c) What is the *y* –intercept of this relation?

(d) State the maximum and minimum values the graph obtains.

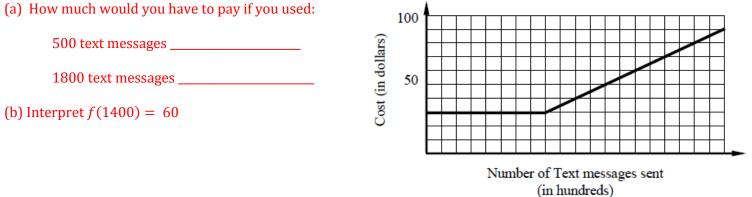
(e) Explain why the graph above represents a function.

2.) Consider the function f(x) = 3(2 - x) - 2. Fill out the function table below for the inputs given and graph the function on the axes provided.

x	3(2-x)-2	(x, y)
-2		
-1		
0		
1		
2		



3.) The following graph represents the cost of a phone plan after a certain number of text messages used in a month. Analyze the graph to answer the following questions.

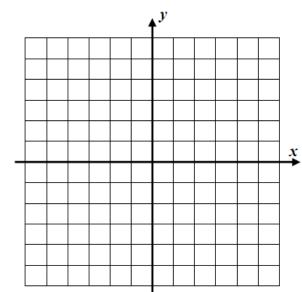


(c) What might have caused the graph to begin increasing at 800 text messages?

- 4.) Consider the following relationship given by the formula $f(x) = \begin{cases} 3 2x & x \le 1 \\ 2x 1 & x > 1 \end{cases}$
- (a) Evaluate each of the following: f(5) = f(-2) =

(b) Carefully evaluate f(1)

(d) Graph y = f(x) on the axes below.



(c) Fill out the table below for the inputs given. Keep in mind which formula you are using.

x	Rule/Calculation	(x, y)
-1		
0		
1		
2		
3		

(e) What is the minimum value of the function? Circle the point that indicates this value on the graph.

Review Section:

5.) An example of an algebraic equation is: [1] $r^2 + 1$ [2] 2a + (n - 1)d[3] 5x = 7 [4] -25x + 100

6.) What is the value of the expression $3x^2 - 4|x| + 6$ when x = -3? [1] -24 [2] -9 [3] 21 [4] 45

7.) Which relation is a function?
[1] {(2,1), (3,1), (4,1), (5,1)}
[2] {(1,2), (1,3), (1,4), (1,5)}
[3] {(2,3), (3,2), (4,2), (2,4)}
[4] {(1,6), (2,8), (3,9), (3,12)}

8.) When $6x^2 - 4x + 3$ is subtracted from $3x^2 - 2x + 3$ the result is: [1] $3x^2 - 2x$ [2] $3x^2 - 6x + 6$ [3] $-3x^2 + 2x$ [4] $-3x^2 - 6x + 6$

9.) Three times the sum of a number and four is equal to five times the number, decreased by two. If x represents the number, which equation is a correct translation of the statement?

 $\begin{bmatrix} 1 \end{bmatrix} 3(x+4) = 5x-2 \\ \begin{bmatrix} 2 \end{bmatrix} 3(x+4) = 5(x-2) \\ \begin{bmatrix} 3 \end{bmatrix} 3x+4 = 5x-2 \\ \begin{bmatrix} 4 \end{bmatrix} 3x+4 = 5(x-2) \\ \end{bmatrix}$

10.) W	Thich value of x is the solution of the equation	2(x-4) + 7 = 3?
[1] 1	[2] 2	
[3] 6	[4] 0	

Name:	Date: Period:	
Algebra I	Graphical Features	3 E

There is a lot of terminology associated with the graph of a function. Many of the terms have names that are descriptive, but still, work is needed to master the ideas.

Exercise #1: The Function y = f(x) is shown graphed below over the interval $-7 \le x \le 7$. (a) Find the maximum and minimum values of the function. State the values of *x* where they occur as well.

(b) What is the *y*-intercept of the function? Explain why a function cannot have more than one *v*-intercept.

(c) Give the *x*-intercepts of the function. These are also known as the function's **zeroes** because they are where f(x) = 0

(d) Would you characterize the function as increasing or decreasing on the domain interval $-5 \le x \le -1$. Explain your answer (e) one additional interval over which the function is increasing and one over which it is decreasing.

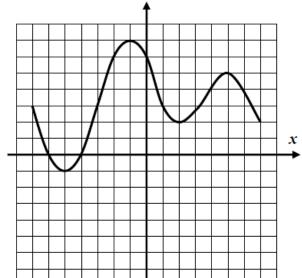
Increasing: _____

Decreasing: _____

(f) The following points are known as turning points. Each can be classified as a relative maximum or a relative minimum. State which you think each point is: (-1,7)

(-5, -1)

(2,2)

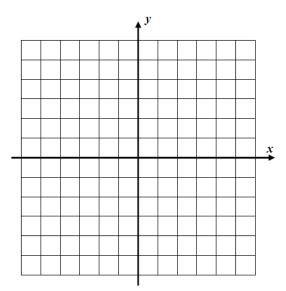


(5,5)

Let's get some more practice with piecewise defined functions and mix in our function terminology while we are at it.

Exercise #2: Consider the piecewise linear function given the equation $f(x) = \begin{cases} x+3 & x \le 1 \\ 6-2x & x > 1 \end{cases}$ (a) Create a table of values for this function below over the interval $-4 \le x \le 4$. Then create a graph on the axes for this function.

x	Rule/Calculation	(x, y)
-4		
-3		
-2		
-1		
0		
1		
2		
3		
4		



(b) State the zeros of the function.

(d) Give the interval over which the function is increasing

Give the interval over which it is decreasing

Increasing: _____

Decreasing: _____

(f) Use your graph to find all solutions to the equation f(x) = 2 Illustrate your solution graphically and find evidence in the table you created.

(e) Give the coordinates of the one turning point and classify it as a relative minimum or maximum.

(c) State the function *y* – intercept

(g) State the interval over which this function is positive. How can you tell this quickly from the graph?

Name: Algebra I	Date:Period:Graphical Features3E HW
1.) The function $y = f(x)$ is shown graphed over the i (a) Evaluate each of the following:	interval $-8 \le x \le 8$
f(-2) = f(8) =	
f(-8) = f(4) =	
(b) Find all the relative maximum and minimum value of the function. State the values of x where they occur as well.	

(c) What are the absolute maximum and minimum values of the function? At what *x* –values do they occur?

(d) What are the x and y – intercept(s) of the function? List each of the following as an ordered pair (x, y)

x –intercept (s): ______ *y* –intercept(s): _____ (zeros)

(e) Give an interval over which the function is increase and one interval which it is decreasing.

Decreasing: _____ Increasing:

(f) Use your graph to find all solutions to the equation f(x) = 3 Illustrate your solution graphically.

(g) Is the function positive or negative on the interval -1 < x < 3? How can you tell quickly?

2.) On the following set of axis, create the graph of a function f(x) with the following characteristics: Passes through the points:

(-8,0) (5, -2) and (8,3)

Has an absolute maximum at f(-4) = 5

Has an absolute minimum at f(2) = -6

Decreasing on the interval $-4 \le x \le 2$

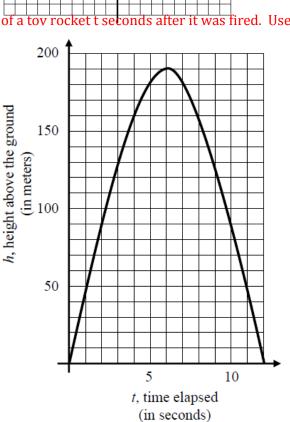
3.) The following graph shows the height, h, above the ground of a tov rocket t seconds after it was fired. Use the graph of h(t) to answer the following questions.

(a) What was the maximum height the rocket reached? After how many seconds?

(b) How many seconds was the rocket in flight?

(c) Interpret h(2) = 90

(d) Give the interval for t over which the height of the rocket is decreasing.



Review Section:

4.) Which expression represents "5 less than twice x"? [1] 2x - 5 [2] 2(5 - x) [3] 5 - 2x [4] 2(x - 5)

5.) A soda container holds $5\frac{1}{2}$ gallons of soda. How many ounces of soda does this container hold?

	1 quart = 32 ounces 1 gallon = 4 quarts	
[1] 44	[2] 17	76
[3] 64	0 [4] 70)4

6.) If the expression $(2y^a)^4$ is equivalent to $16y^8$, what is the value of a? [1] 12 [2] 32

[1] 12 [2] 32 [3] 2 [4] 4

7.) When $2x^2 - 3x + 2$ is subtracted from $4x^2 - 5x + 2$, the result is [1] $2x^2 - 2x$ [2] $-2x^2 - 8x + 4$

- $[3] -2x^2 + 2x \qquad [4] 2x^2 8x + 4$
- 8.) Solve the inequality -5(x 7) < 15 algebraically for x.

Name:	Date:	_ Period:	
Algebra I	Exploring Function	S	3F

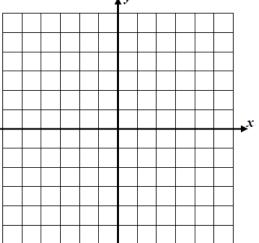
Graphing calculators are powerful tools in our exploration of functions and the rules that define them. Because calculators are so good at doing calculations, it is fairly easy to have them evaluate **expressions** that are the **rules** for generating the **outputs** for the functions. Throughout this entire lesson, we will assume that you have a calculator that can do the following:

GRAPHING CALCULATOR ESSENTIALS		
1. A TABLE APP	AND	2. A GRAPHING APP

We can use our calculator to help us produce tables that are very useful in plotting graphs and exploring functions.

Exercise #1: Consider the linear function $f(x) = \frac{1}{2}x + 2$. Do the following by using your graphing calculators table function.

(a) Evaluate f(-6), f(0), and f(8).



(b) Explore the table to determine the value of x for which f(x) = 11.

(c) Use the table to fill out the following table and graph the function
on the grid for the interval $-6 \le x \le 6$.

x	У	(x, y)
-6		
-4		
-2		
0		
2		
4		
6		

(d) Graph the linear function g(x) = 5 - x on the same set of axes and find where the two lines intersect.

x	У	(x, y)
-6		
-4		
-2		
0		
2		
4		
6		

(e) Show that the point you found in part d is a solution to both equation:

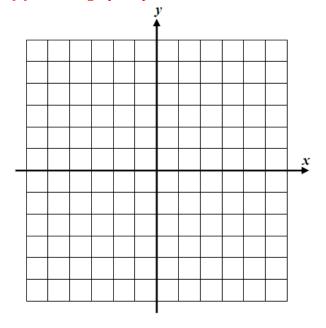
$$y = \frac{1}{2}x + 2$$
 and $y = 5 - x$

The calculator can do the heavy lifting with the calculations, while we examine the results. Always be careful when entering algebraic expressions on your calculator. Let's take a look at a **quadratic function** using the graphing calculator.

Exercise #2: Consider the function $y = (x - 1)^2 - 4$ over the interval $-1 \le x \le 4$ Do the following with the use of tables on your graphing calculator.

(a) Create a table of values for this function.

(b) Create a graph of your function on the axes below.



(c) What are the function's minimum and maximum values on this interval?

(d) Over what interval is the function negative?

(e) For your graph, state the interval over which the function is increasing.

(f) How can this graph help to solve the equation $(x - 1)^2 - 4 = -3$? Can you solve this by looking at your table?

Exercise #3: Which of the following is a point where $y = \frac{3}{2}x + 7$ and y = -5x - 6 intersect? [1] (0,7) [2] (-1,-1) [3] (-2,4) [4] (2,10) Name:____ Algebra I

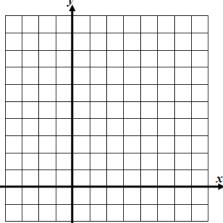
Date:	Period:	
Exploring Functions		3F HW

1.) Consider the function $g(x) = 3x^2 + 2x - 4$ Evaluate the following using your graphing calculator. (a) g(-2) = (b) g(0) =

(c)
$$g(4) =$$
 (d) $g(15) =$

2.) Given the function $f(x) = x^2 - 2x + 1$ fill in the missing values in the table then using the table graph the function on the grid for the interval. Use your calculator.

x	У	(x, y)
-2		
		(-1,4)
0		
	0	
2		
3		
	9	



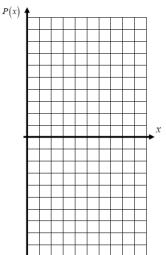
3.) Which of the following values of x will make the equation $3(x - 2)^2 - 4 = 23$ true? Show the table on your calculator that justifies your choice.

- [1] x = 1 [2] x = 5
- [3] x = 4 [4] x = 0

4.) Profits for the upcoming year for a shipping company have been quantified and put into the equation $P(x) = \frac{1}{2}(x-2)^2 - 8$ where x is the number of packages shipped in thousands and P(x) is the corresponding profit in millions of dollars.

(a) Use your calculator to fill out the following table and graph the function on the grid to the right.

x	P(x)	(x, y)
0		
2		
4		
6		
8		
10		



(b) Over what interval is P(x) < 0? What does this interval represent?

(c) Evaluate P(0) What might this stand for?

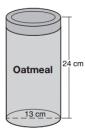
(d) Explore the table to determine the value of x for which P(x) = 0 What might this stand for?

5.) After placing an equation into his calculator Rob got the following table. He then determines that x = 6 when f(x) = -4. Is he correct? Explain your answer.

x	f(x)
-4	6
-2	3
0	-1
2	-4

Review Section:

6.) Oatmeal is packaged in a cylindrical container, as shown in the diagram. The diameter of the container is 13 centimeters and its height is 24 centimeters. Determine, in terms of π , the volume of the cylinder $V = \pi r^2 h$.



7.) What is the quotient of:
$$\frac{8x^5 - 2x^4 + 4x^3 - 6x^2}{2x^2}$$

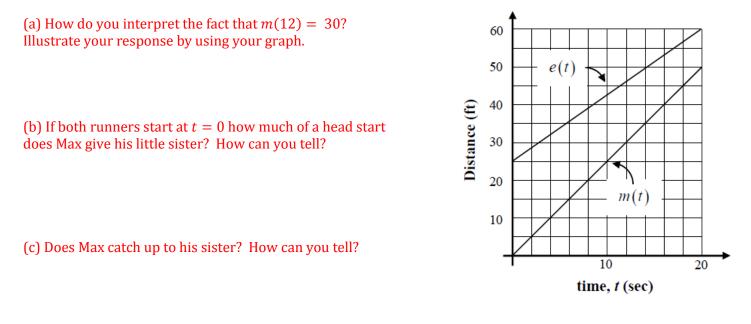
8.) Marcy determined that her father's age is four less than three times her age. If x represents Marcy's age, which expression represents her father's age?

[1] 3x - 4	[2] 3(x-4)
[3] 4x - 3	[4] 4 - 3x

Name:	Date: Period:	
Algebra I	Average Rate of Change	3G

Functions are rules that give us **outputs** when we supply them with **inputs**. Very often, we want to know how **fast** the outputs are changing compared to a change in the input values. This is referred to as the **average rate of change** of a function.

Exercise #1: Max and his younger sister Evie are having a race in the backyard. Max gives his sister a head start and they run for 20 seconds. The distance they are along in the race, in feet, is given below with Max's distance given by the function m(t) and Evie's distance given by the function e(t)



(d) How far does Max run during the 20 second race? How far does Evie run? What calculation can you do to find Evie's distance?

(e) How fast do both Evie and Max travel? In other words, how many feet do each of them run per second? Express your answer in decimals and attach units.

MAX'S SPEED (FEET PER SECOND) EVIE'S SPEED (FEET PER SECOND) In the first exercise we were calculating the **rate** that the **function's output (y-values)** were changing compared to the **function's input (or x-values)**. This is known as finding the **average rate of change** of the function. You might think you've seen this before. And you have.

Exercise #2: Finding the average rate of change is the same as finding the ______ of a line.

There is, of course, a formula for finding average rate of change. Let's get it out of the way.

AVERAGE RATE OF CHANGE For the function y = f(x), the average rate that f(x) changes from x = a to x = b is given by: $\frac{f(b) - f(a)}{b - a} = \frac{\text{how much the y-values have changed}}{\text{how much the x-values have changed}}$

Exercise #3: Consider the function given by $f(x) = x^2 + 3$ Find its average rate of change from x = -1 to x = 3 Carefully show the work that leads to your final answer.

Exercise #4: The function h(x) is given in the table below. Which of the following gives its average rate of change over the interval $2 \le x \le 6$? Show your calculations that lead to your answer.

$[1] - \frac{5}{2}$	$[2] \frac{3}{4}$	x	h(x)
7		0	10
$[3] - \frac{7}{6}$	[4] -1	2	9
		4	6
		6	3

Exercise #5: A function is represented by the table provided. What is the average rate of change for the table provided?

x	f(x)
2	0
5	1
8	2
11	3
14	4

Exercise #6: Frances is selling glasses of lemonade. The function $g(t) = \frac{t^2+4}{2}$ models the number of glasses she has sold g after t -hours. What is the average rate at which she is selling lemonade between t = 2 and t = 6 hours. Include proper units in your answer.

Name:	Date: Period:	
Algebra I	Average Rate of Change30	G HW

1.) Consider the function given by $f(x) = 9 - x^2$. Find its average rate of change between the following points. Carefully show the work that leads to your final answer.

(a) x = 0 to x = 3 (b) x = -1 to x = 5 (c) x = -2 to x = 2

2.) The function f(x) is given in the table below. Find its average rate of change between the following points. Show the calculations that lead to your answer.

x	f(x)	(a) $x = -3$ to $x = 1$	(b) $x = 0$ to $x = 4$
-3	7		
0	-2		
1	3		
4	-8		

3.) The function f(x) is given in the graph below. Find its average rate of change between the following points. Show the calculations that lead to your answer.

(a) x = -6 to x = 4 (b) x = -2 to x = 2

4.) The following table shows the number of points the Arlington girls team scored in their last basketball game where *t* is the time passed in minutes and f(t) the total number of points scored after *t* minutes. (a) What was the average rate they were shooting in the first half of the game? Be sure to include proper units in your answer.

t	f(t)
0	0
8	30
16	48
24	55
32	64

(b) What was their average rate over the whole game?

(c) Given your answers above which half of the game do you feel they had a better rate of scoring? Explain.

5.) Consider the function given by f(x) = 6x + 5(a) Find its average rate of change from x = 1 to x = 5

(b) Find its average rate of change from x = -2 to x = 6

(c) The average rate of change for this function is always 6 (as you should have found in the first two parts of the problem). What type of function has a constant average rate of change? What do we call this average rate of change in this case? Search the Internet if needed.

Review Section:	
6.) What is the product of (3x	(x + 2) and $(x - 7)$?
$[1] 3x^2 - 14$	[2] $3x^2 - 5x - 14$
$[3] \ 3x^2 - 19x - 14$	[4] $3x^2 - 23x - 14$

- 7.) If five times a number is less than 55, what is the greatest possible integer value of the number? [1] 12 [2] 11
- [1] 12 [2] 12 [3] 10 [4] 9

8.) The length of one side of a square is 13 feet. What is the length, to the nearest foot, of a diagonal of the square?
[1] 13 [2] 18 [2] 18 [4] 26 [4] 26 [4] 26 Pythagorean Theorem to find the length of the diagonal.

9.) If n is an odd integer, which equation can be used to find three consecutive odd integers whose sum is -3? [1] n + (n + 1) + (n + 3) = -3[2] n + (n + 1) + (n + 2) = -3[3] n + (n + 2) + (n + 4) = -3[4] n + (n + 2) + (n + 3) = -3

10.) When $8x^2 + 3x + 2$ is subtracted from $9x^2 - 3x - 4$, the result is: [1] $x^2 - 2$ [2] $17x^2 - 2$ [3] $-x^2 + 6x + 6$ [4] $x^2 - 6x - 6$

N	lame:	
A	lgebra	Ι

Ultimately, all functions do is convert inputs into outputs. So, each function has two **sets** associated with it. Those things that serve as **inputs** and those things that serve as **outputs**. These sets are given names.

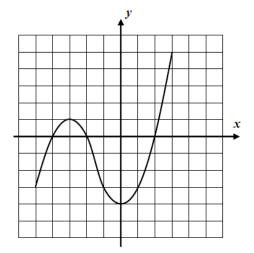
THE DOMAIN AND RANGE OF A FUNCTION

- 1. The domain of a function is the set of all inputs for which the function rule can give an output.
- 2. The range of a function is the set of all outputs for which there is an input that results in them.

Exercise #1: Consider the function y = f(x) shown on the graph. (a) Evaluate each of the following:

$$f(-3) = f(1) = f(3) =$$

(b) Can the function rule, given by the graph, give you a value when x = 5? If so, what is it? If not, why not?



(c) Is x = 5 in the domain of the function?

(d) Give two other values of *x* that are **not** in the **domain** of the function.

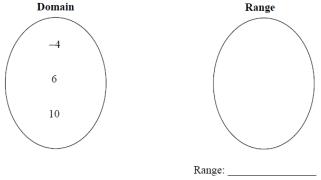
(e) Circle the following *y*-values that are in the **range** of the function? Show evidence on your graph.

$$y = 0 \qquad \qquad y = 6 \qquad \qquad y = -1$$

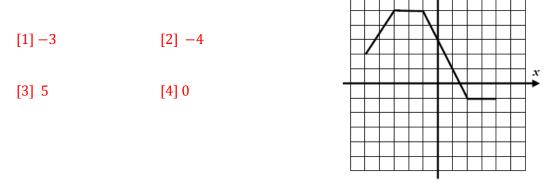
 $y = 3 \qquad \qquad y = -5 \qquad \qquad y = 4$

(f) Write the domain and range of this function using a single inequality. **DOMAIN RANGE**

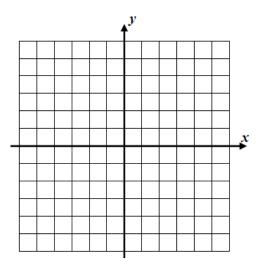
Exercise #2: Given the function $f(x) = \frac{x}{2} - 3$ and the domain shown below, fill in the range. Write the set in *roster notation*.



Exercise #3: Which of the following values is *not* in the domain of the function f(x) shown below? Illustrate your thinking by marking points on the graph

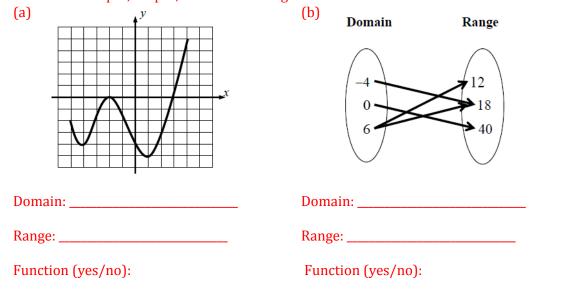


Exercise #4: Consider the piecewise linear function given by the formula $f(x) = \begin{cases} \frac{-(x+2)}{2} & -4 \le x \le 2\\ 4x - 10 & 2 \le x \le 4 \end{cases}$ Determine the functions range.

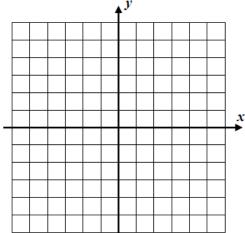


Name:	Date:	Period:	
Algebra I	Domain & Ra	nge of a Function	3H HW

1.) In each of the following, state the domain and range; then decide if it's a function or not. Be sure to explain using words such as input, output, domain and range!

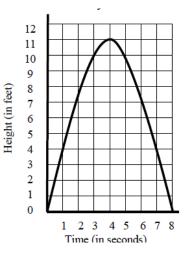


2.) Consider the piecewise linear function given by the formula $f(x) = \begin{cases} 2-3x & -1 \le x \le 1 \\ x-2 & 1 < x \le 3 \end{cases}$. Determine the function's domain and range. Draw a graph of the function to fully justify your answer. Use tables on your calculator to help graph.



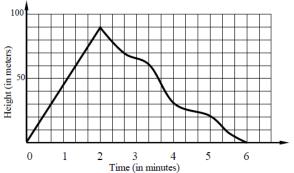
3.) The graph below represents the height of a ball over the interval $0 \le t \le 8$ After how many seconds was the ball 12 feet off of the ground? Explain your answer.

What does your answer indicate about the range of this function?



4.) The following graph represents the height above the ground versus time at a resort as Thomas rides his favorite ski slope.

(a) State the domain and, in your own words, what the domain represents.



(b) State range and, in your own words, what the range represents.

(c) What might Thomas have been doing for the interval $0 \le t \le 2$? What was his average rate of change? Use proper units in your answer.

(d) What might Thomas have been doing for the interval $2 \le t \le 6$? What was his average rate of change? Use proper units in your answer and compare to what you found in (c).

Review Section: 5.) Solve algebraically for x: 3(x + 1) - 5x = 12 - (6x - 7)

6.) Carla bought a dress at a sale for 20% off the original price. The sale price of the dress was \$28.80. Find the original price of the dress, in dollars.

7.) A model rocket is launched into the air from ground level. The height, in feet, is modeled by $p(x) = -16x^2 + 32x$, where x is the number of elapsed seconds. What is the total number of seconds the model rocket will be in the air?

	[2] 2
[3] 0	[4] 16

8.) Last year, Nick rode his bicycle a total of 8000 miles. To the nearest yard, Nick rode an average of how many yards per day?

1 mile = 1760 yards
1 year = 365 days

9.) Given the relation $B = \{(5,2), (7,4), (9,10), (x,5)\}$ Which of the following values for x will make relation B a function?

[1] 7	[2] 9
[3] 4	[4] 5

10.) The table below shows the average diameter of a pupil in a person's eye as he or she grows older. What is the average rate of change, in millimeters per year, of a person's pupil diameter from age 20 to age 80?

[1]	2.4
[2]	0.04
[3]	-2.4
[4]	-0.04

Age (years)	Average Pupil Diameter (mm)
20	4.7
30	4.3
40	3.9
50	3.5
60	3.1
70	2.7
80	2.3